

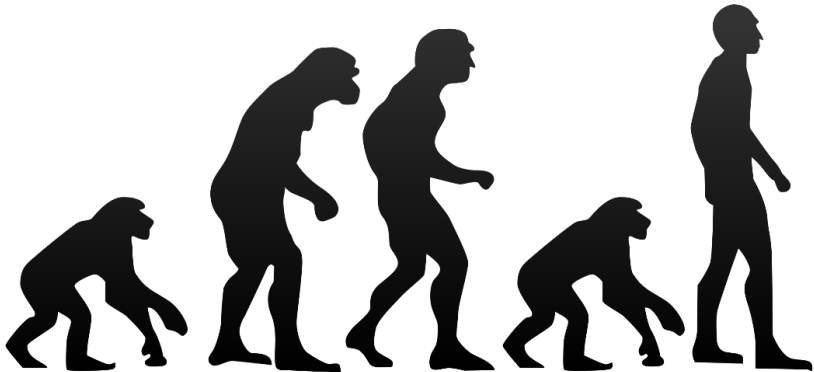
# Regression Verification: Final Report

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within the  
*Projektgruppe Formale Methoden der Softwareentwicklung*

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# How to prevent regressions in software development?



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## Formal Verification

Formally prove correctness of software  
⇒ Requires formal specification

## Regression Testing

Discover new bugs by testing for them  
⇒ Requires test cases

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## Formal Verification

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## Regression Verification

Formally prove there are no new bugs

# Project Objectives

- ① Develop a tool for Regression Verification for recursive programs in a simple imperative programming language
- ② Evaluate how well our approaches work for different examples
- ③ Extend the tool to work with more programs and to be more general

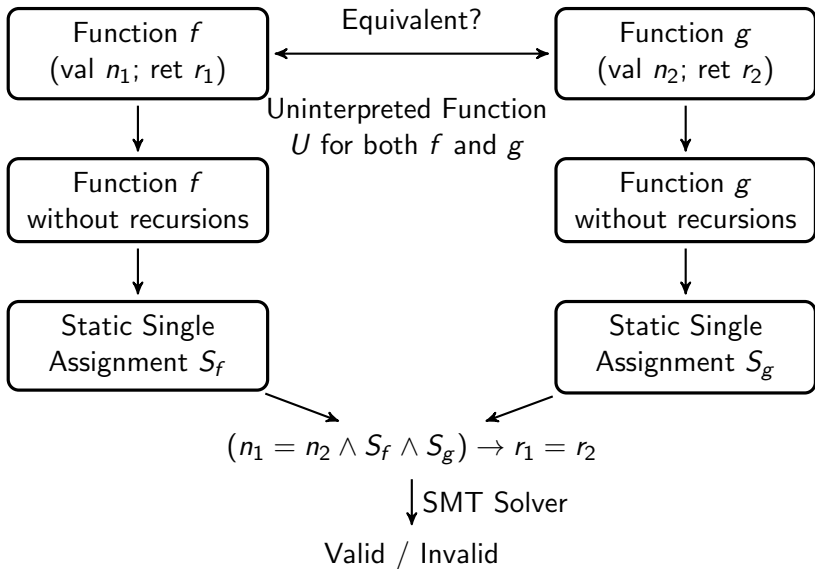
# Regression Verification

## Formally prove there are no new bugs

- Goal: Proving the equivalence of two **closely related** programs
- No formal specification or test cases required
- Instead use old program version as reference
- Approach by Strichman & Godlin for C using CBMC
- Here: Tool for **function equivalence** in a simple language using SMT solvers

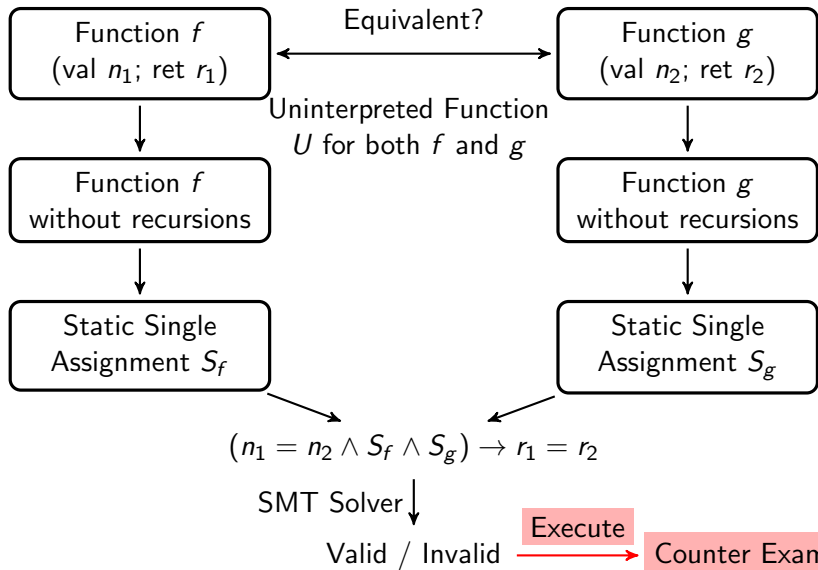
# Function Equivalence

Existing approach by Strichman & Godlin



# Extensions

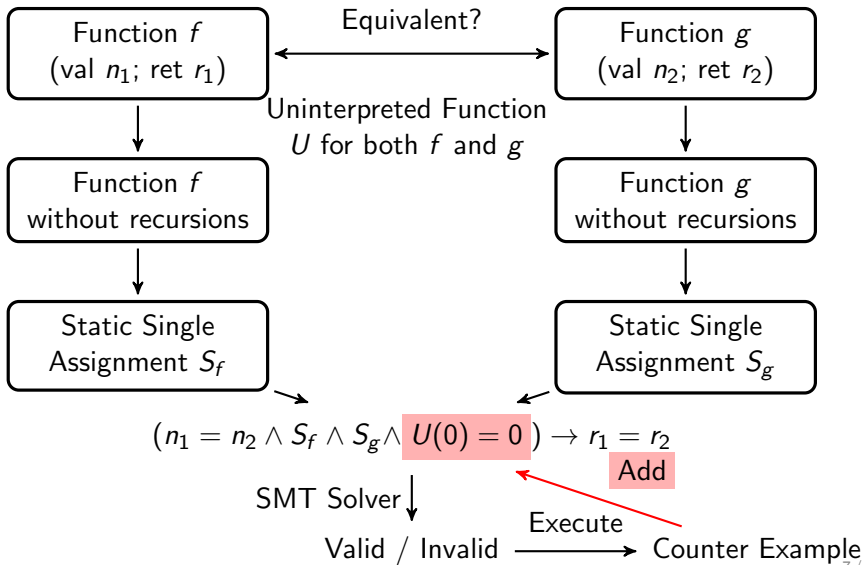
## Finding Counter Examples





# Extensions

## Determining Corner Cases



# Automatic Transition Relation Inference

## Recursive approach

- So far recursions replaced by Uninterpreted Function
- Now approximate the recursive calls with a mutual **Transition Relation** (TR)
- Encode behaviour of both functions for every path into TR
- Assuming TR assert that functions behave equally
- Infer TR automatically using SMT solvers

## Working examples

- Different paths for same input
- Inlined recursions
- Recursive versus tail recursive implementation

# Automatic Transition Relation Inference

## Transition Relation Approximation

$$TR_{real}(p_1, r_1, p_2, r_2) = true \Leftrightarrow r_1 = f(p_1) \wedge r_2 = g(p_2)$$

$p_1$  parameter to recursive call of  $f$

$r_1$  result of recursive call of  $f$

$p_2$  parameter to recursive call of  $g$

$r_2$  result of recursive call of  $g$

# Automatic Transition Relation Inference

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$r_2$  parameter to recursive call of  $g$

$p_2$  result of recursive call of  $g$

Approximation:  $TR \supseteq TR_{real}$

Examples:

- Identical recursion step:

$$TR(p_1, r_1, p_2, r_2) = (p_1 = p_2 \rightarrow r_1 = r_2)$$

- Functions off by one:

$$TR(p_1, r_1, p_2, r_2) = (p_1 = p_2 \rightarrow r_1 = r_2 + 1)$$

Results are not specified, but relationship of results!

## Automatic Transition Relation Inference

```
int sum1(int n) {  
    if (n <= 0)  
        return 0;  
    int r = n + sum1(n-1);  
    return r;  
}
```

```
int sum2(int n , int a) {  
    if (n <= 0)  
        return a;  
    int r = sum2(n-1 , n+a);  
    return r;  
}
```

## Automatic Transition Relation Inference

```
int sum1(int n) {
    if (n <= 0)
        return 0;
    int r = n + sum1( n-1 );
    return r;
}

int sum2(int n, int a) {
    if (n <= 0)
        return a;
    int r = sum2( n-1 , n+a );
    return r;
}
```

- Paths (two out of four possible):

$(n \leq 0)$

$\rightarrow TR(n, 0, n, a_2, a_2)$

## Automatic Transition Relation Inference

```
int sum1(int n) {
    if (n <= 0)
        return 0;
    int r = n + sum1(n-1);
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    if (n <= 0)
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```

- Paths (two out of four possible):

$(n \leq 0) \rightarrow TR(n, 0, n, a_2, a_2)$

$(n > 0 \wedge TR(n-1, r_1, n-1, n+a_2, r_2)) \rightarrow TR(n, n+r_1, n, a_2, r_2)$

## Automatic Transition Relation Inference

```
int sum1(int n) {
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}
```

- Paths (two out of four possible):

$(n \leq 0) \rightarrow TR(n, 0, n, a_2, a_2)$

$(n > 0 \wedge TR(n-1, r_1, n-1, n+a_2, r_2)) \rightarrow TR(n, n+r_1, n, a_2, r_2)$

- Show the functions behave equally:

$\exists TR.(n_1 = n_2 \wedge a_2 = 0 \wedge TR(n_1 - 1, r_1, n_2 - 1, n_2 + a_2, r_2))$

$\rightarrow ite(n_1 \leq 0, 0, n_1 + r_1) = ite(n_2 \leq 0, a_2, r_2)$



## Automatic Transition Relation Inference

```
int sum1(int n) {
  if (n <= 0)
    return 0;
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int sum2(int n, int a) {
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    return a;
  int r = sum2(n-1, n+a);
  return r;
}
```

- Paths (two out of four possible):

$(n \leq 0) \rightarrow TR(n, 0, n, a_2, a_2)$

$(n > 0 \wedge TR(n-1, r_1, n-1, n+a_2, r_2)) \rightarrow TR(n, n+r_1, n, a_2, r_2)$

- Show the functions behave equally:

$\exists TR.(n_1 = n_2 \wedge a_2 = 0 \wedge TR(n_1 - 1, r_1, n_2 - 1, n_2 + a_2, r_2))$

$\rightarrow ite(n_1 \leq 0, 0, n_1 + r_1) = ite(n_2 \leq 0, a_2, r_2)$

- Resulting TR predicate found by SMT solver Eldarica:

$TR(n_1, r_1, n_2, a_2, r_2) = (n_1 = n_2 \wedge r_1 = r_2 - a_2)$

# Automatic Invariant Inference

## Iterative approach

- Loops instead of recursions
- Coupling invariant for both programs
- Completely automatic translation to SMT2

## Working examples

- Synchronised loops
- Loosely synchronised loops
- Conditional and relational equivalence

## Automatic Invariant Inference

```
int f1(int n) {  
    int r = 0;  
    if (n == 0) return 1;  
    while (n > 0) {  
        n /= 10; r++;  
    }  
    return r;  
}
```

```
int f2(int n) {  
    int r = 1;  
    while (true) {  
        if (n < 10) return r;  
        if (n < 100) return r+1;  
        if (n < 1000) return r+2;  
        if (n < 10000) return r+3;  
        n /= 10000;  
        r += 4;  
    }  
}
```

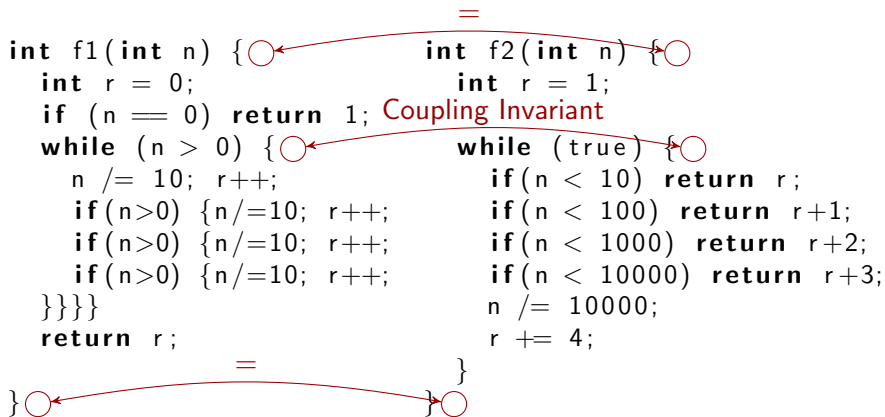
## Automatic Invariant Inference

```
int f1(int n) {  
  int r = 0;  
  if (n == 0) return 1;  
  while (n > 0) {  
    n /= 10; r++;  
    if(n>0) {n/=10; r++;  
    if(n>0) {n/=10; r++;  
    if(n>0) {n/=10; r++;  
  }}}}  
  return r;  
}
```

```
int f2(int n) {  
  int r = 1;  
  while (true) {  
    if(n < 10) return r;  
    if(n < 100) return r+1;  
    if(n < 1000) return r+2;  
    if(n < 10000) return r+3;  
    n /= 10000;  
    r += 4;  
  }  
}
```

Inlining preserves semantics

# Automatic Invariant Inference



Inlining preserves semantics

## Automatic Invariant Inference

$$(n_1 = n_2 \wedge \text{init}_1(n_1, r_1, n'_1, r'_1) \wedge \text{init}_2(n_2, r_2, n'_2, r'_2)) \rightarrow \\ \text{inv}(n'_1, r'_1, n'_1, r'_1, n'_2, r'_2, n'_2, r'_2)$$

## Automatic Invariant Inference

$$(n_1 = n_2 \quad \wedge \text{init}_1 \wedge \text{init}_2) \rightarrow \text{inv}$$

$$(\text{inv} \wedge \text{guard}_1 \wedge \text{guard}_2 \wedge \text{step}_1 \wedge \text{step}_2) \rightarrow \text{inv}$$

$$(\text{inv} \wedge \text{guard}_1 \wedge \neg \text{guard}_2 \wedge \text{step}_1) \rightarrow \text{inv}$$

$$(\text{inv} \wedge \neg \text{guard}_1 \wedge \text{guard}_2 \wedge \text{step}_2) \rightarrow \text{inv}$$

$$(\text{inv} \wedge \neg \text{guard}_1 \wedge \neg \text{guard}_2 \wedge \text{post}_1 \wedge \text{post}_2) \rightarrow \text{result}_1 = \text{result}_2$$

## Automatic Invariant Inference

$$(n_1 = n_2 \quad \wedge \text{init}_1 \wedge \text{init}_2) \rightarrow \text{inv}$$

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$$(\text{inv} \wedge \neg \text{guard}_1 \wedge \text{guard}_2 \wedge \text{step}_2) \rightarrow \text{inv}$$

$$(\text{inv} \wedge \neg \text{guard}_1 \wedge \neg \text{guard}_2 \wedge \text{post}_1 \wedge \text{post}_2) \rightarrow \text{result}_1 = \text{result}_2$$

- Automatically inferred coupling loop invariant:  
(Using Eldarica again)

$$\begin{aligned} & (n_1 > 0 \rightarrow (n_1 = n_2 \wedge r_1 + 1 = r_2)) \\ & \wedge (n_2 \leq 0 \rightarrow \text{return}_2 = r_1) \\ & \wedge n_1 \geq n_2 \end{aligned}$$



## Automatic Invariant Inference

$$(n_1 = n_2 \quad \wedge \text{init}_1 \wedge \text{init}_2) \rightarrow \text{inv}$$

$$(\text{inv} \wedge \text{guard}_1 \wedge \text{guard}_2 \wedge \text{step}_1 \wedge \text{step}_2) \rightarrow \text{inv}$$

$$(\text{inv} \wedge \text{guard}_1 \wedge \neg \text{guard}_2 \wedge \text{step}_1) \rightarrow \text{inv}$$

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- Compare to loop invariant:  $n = \frac{n_0}{10^r}$
- Coupling invariant is linear and inferable!

# Conclusion

## Regression Verification

- Initial approach limited to strongly coupled recursions or user feedback
- Automatic Transition Relation inference: More powerful, using recent techniques in SMT solvers like Z3 and Eldarica
- Automatic Invariant inference: Automated approach for loops

## Future Work

- More challenging examples
- Real Programming Language (Java)