

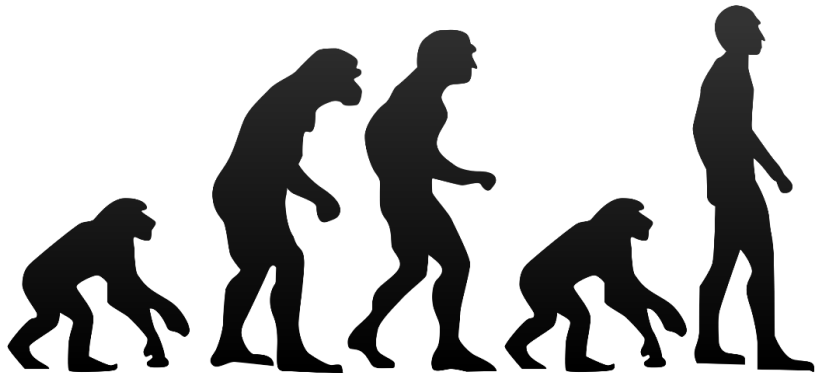
Automating Regression Verification

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How to prevent regressions in software development?



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Formal Verification

Formally prove correctness of software
⇒ Requires formal specification

Regression Testing

Discover new bugs by testing for them
⇒ Requires test cases

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- Goal: Proving the equivalence of two **closely related** programs
- No formal specification or test cases required
- Instead use old program version as reference
- Tools for **proving function equivalence** in a simple programming language using SMT solvers

Overview

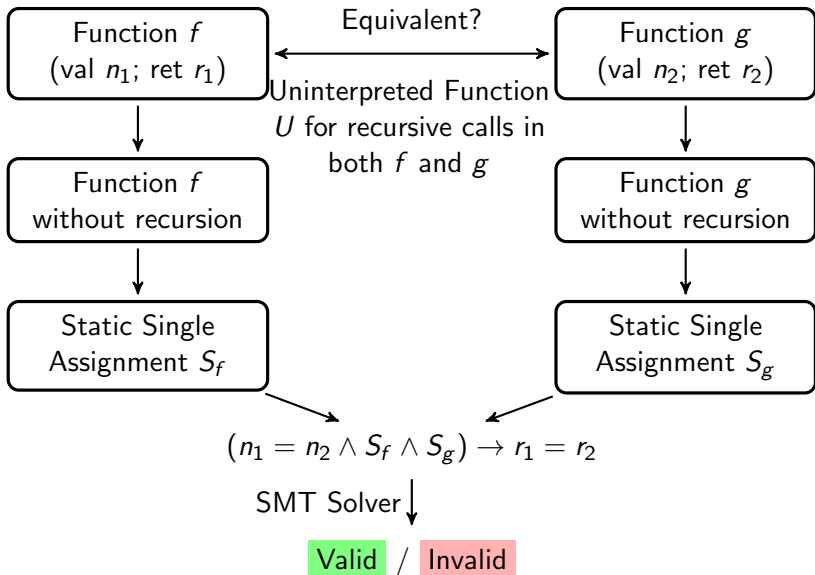
- ① Overapproximation using Uninterpreted Functions
- ② Approximation using Uninterpreted Predicates
- ③ Results and Future Work

Overview

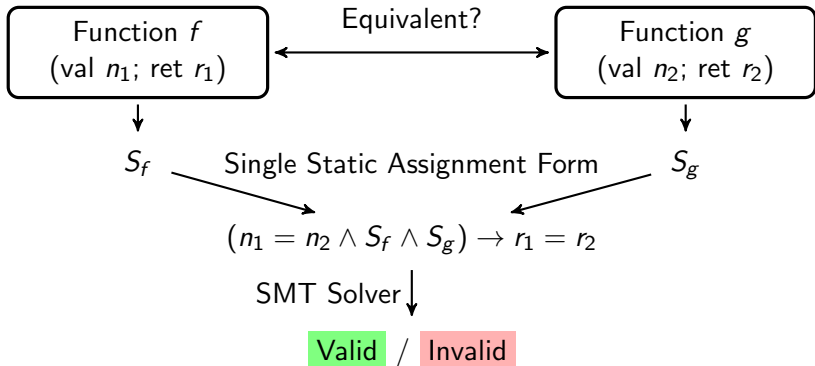
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Function Equivalence

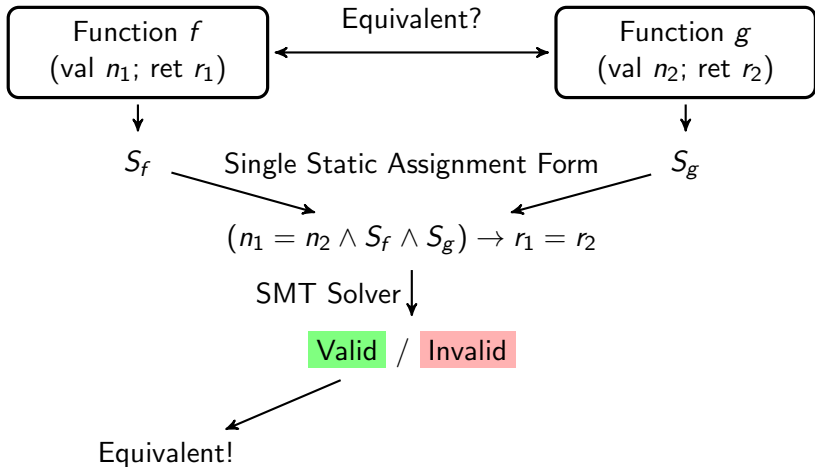
Existing approach by Strichman & Godlin



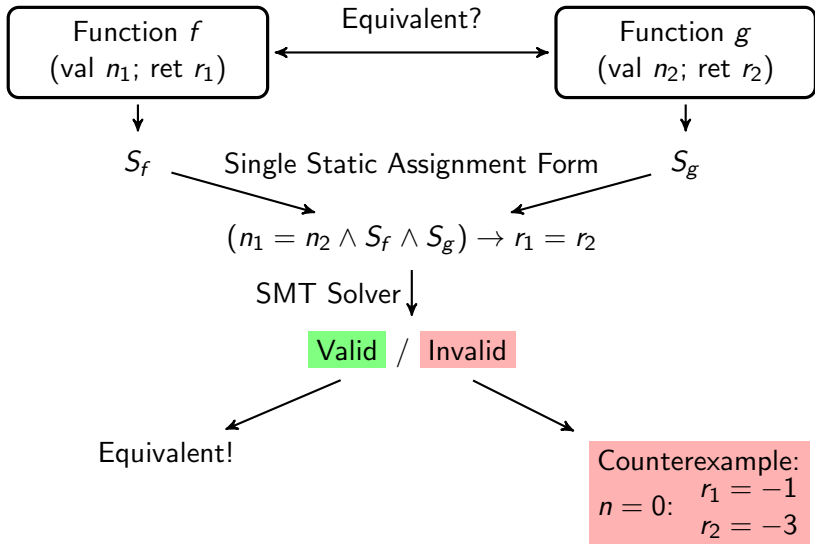
Our Contribution: Extensions



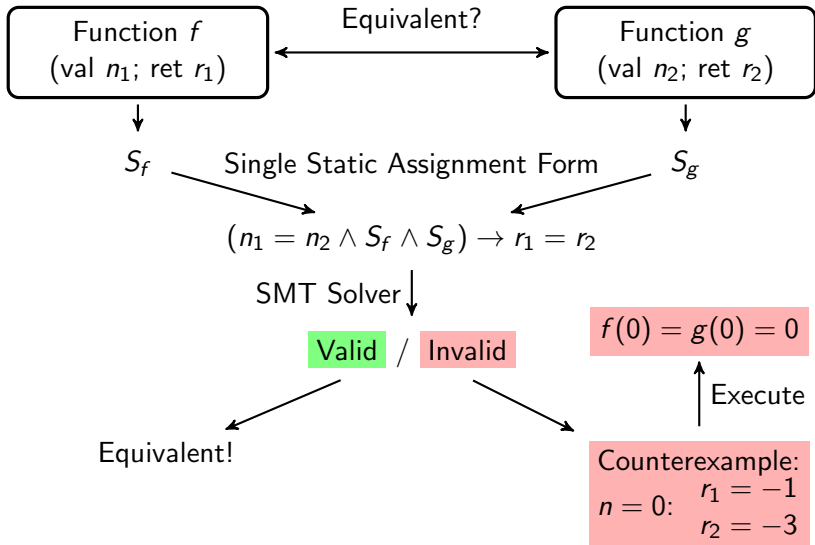
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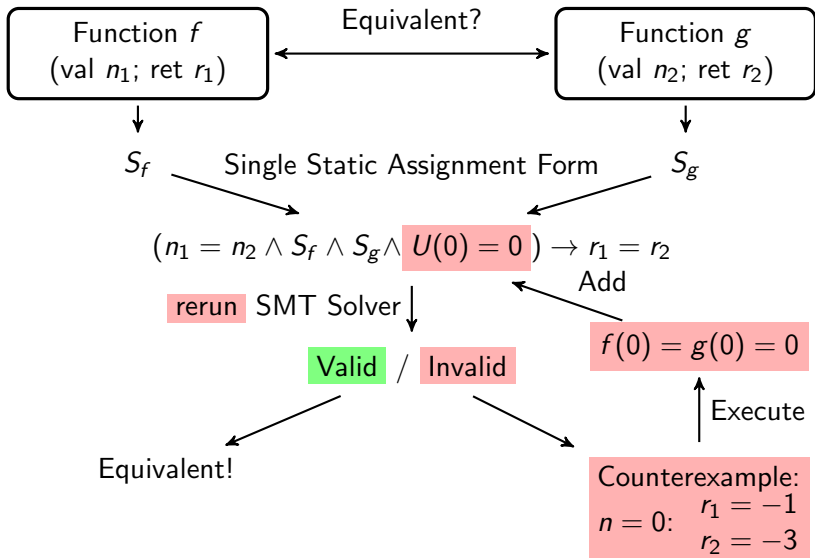
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Overapproximation using uninterpreted functions

Approach

- Run the programs with input gathered from counterexamples
- Detect whether CE is spurious or not
- If spurious: Add additional constraints to the uninterpreted function

⇒ Is a simple form of *Counter Example Guided Abstraction Refinement (CEGAR)*

Successful when

- Finite number of constraints on the uninterpreted function imply equivalence
- These are often the “base cases” of recursive implementations

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Approximation using Uninterpreted Predicates

First approach (just shown)

- Overapproximate recursion by uninterpreted Function U :

$$\forall U. \text{constraints}(U) \wedge S_f \wedge S_g \wedge \dots \rightarrow r_1 = r_2$$

New approach

- Infer a predicate C which couples recursive calls:

$$\exists C. (C(\dots) \wedge \dots \rightarrow r_1 = r_2) \wedge \text{“}C \text{ couples } f \text{ and } g\text{”}$$

- Use state-of-the-art SMT solvers (Eldarica, Z3) to automatically find such a C or prove that it does not exist

⇒ Example will show loops with coupling loop invariants

Automatic Invariant Inference

```
int f1(int n) {  
    int r = 0;  
    if (n == 0) return 1;  
    while (n > 0) {  
        n /= 10; r++;  
  
    }  
    return r;  
  
}
```

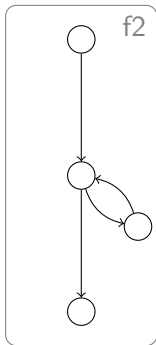
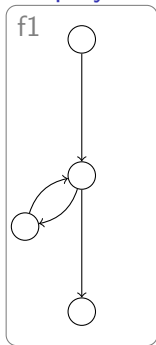
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```
int f2(int n) {  
    int r = 1;  
    while (true) {  
        if(n < 10) return r;  
        if(n < 100) return r+1;  
        if(n < 1000) return r+2;  
        if(n < 10000) return r+3;  
        n /= 10000;  
        r += 4;  
    }  
}
```

Automatic Invariant Inference

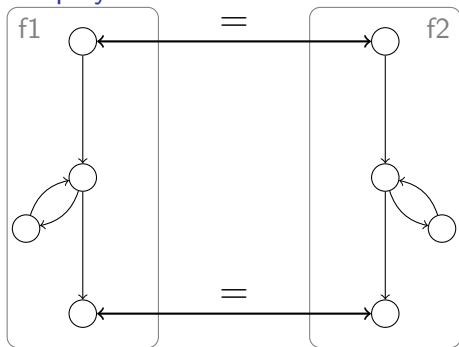
Loop synchronisation



- **To show:** Equal input gives equal output

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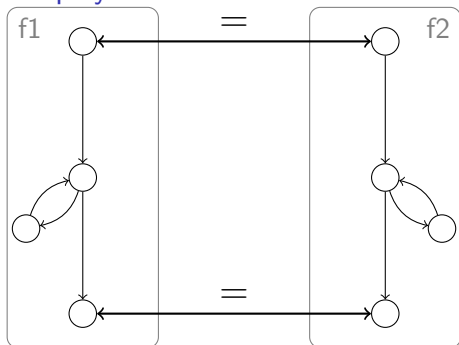
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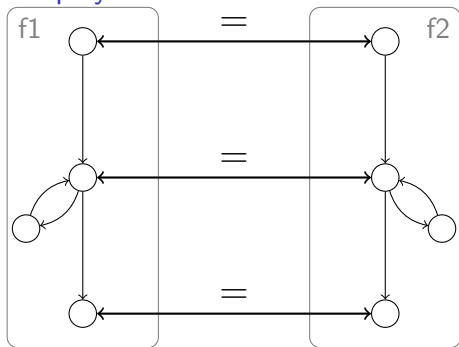
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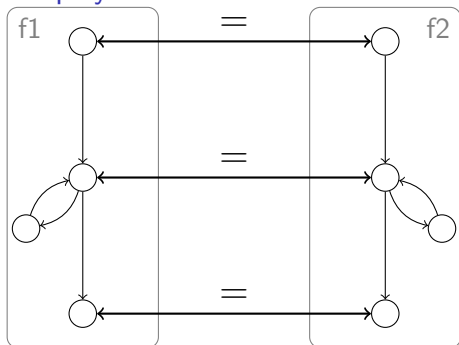
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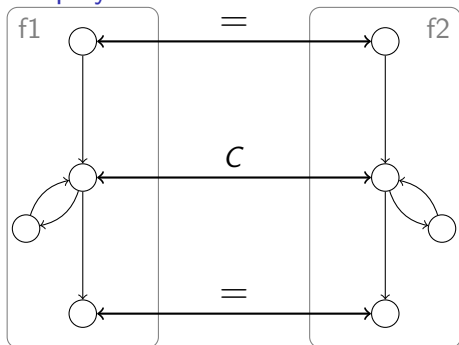
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- **To show:** Equal input gives equal output
- Loops are **synchronised**
- ... at least loosely synchronised

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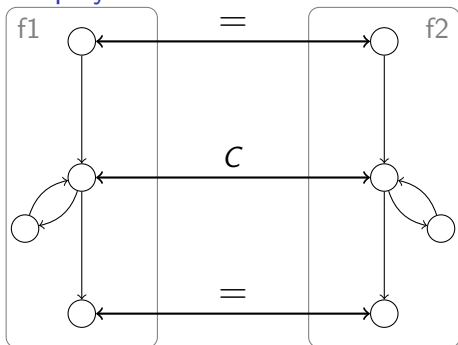
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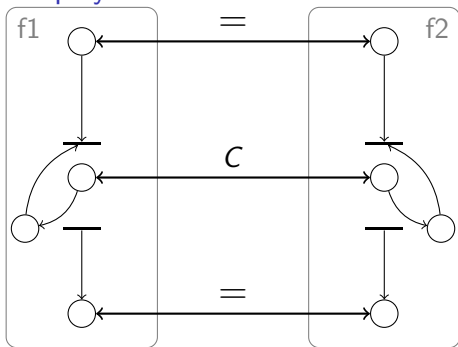
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- ⇒ Use C as **loop invariant** for **both** programs.
(\rightarrow coupling invariant)

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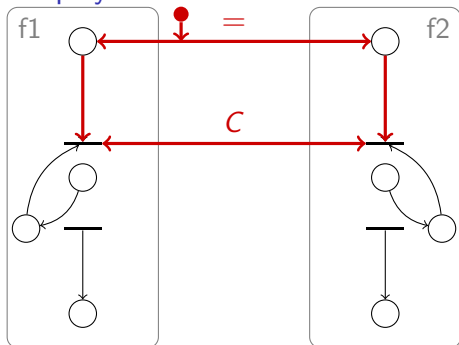
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(→ *coupling invariant*)

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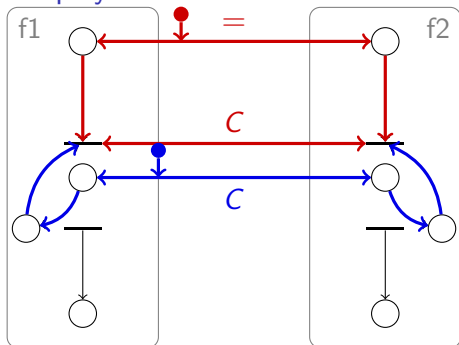
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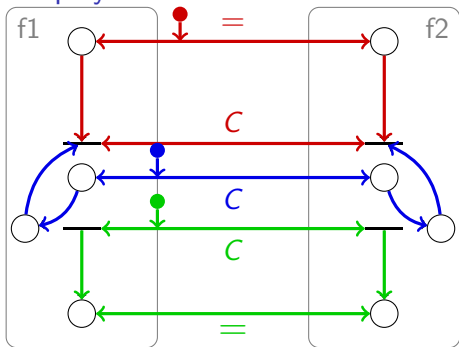
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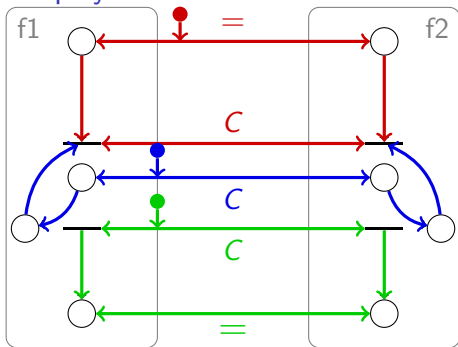


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Automatic Regression Verification:

Do not specify C but infer it automatically.

Automatic Invariant Inference

Three cases to consider:

- ① Initially coupling loop invariant C holds
- ② After both loop steps (or one if other finished), C holds
- ③ After both loops finished, C implies equality of results

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Automatically inferred coupling loop invariant:
(Using Eldarica)

$$\begin{aligned} & (n_1 > 0 \rightarrow (n_1 = n_2 \wedge r_1 + 1 = r_2)) \\ & \wedge (n_2 \leq 0 \rightarrow \text{return}_2 = r_1) \\ & \wedge n_1 \geq n_2 \end{aligned}$$

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- Compare to loop invariant: $n = \frac{n_0}{10^r}$
- Coupling invariant is not trivial, but linear and inferable!

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Evaluation and Results

Approaches implemented for a subset of C: **simplRV**, **Rêve**

Usable with webinterface: <http://formal.iti.kit.edu/improve/deduktionstreffen2014/>

Rêve evaluation (uninterpreted predicates)

- 32 short benchmarks of integer programs (10-50 lines)
- Collected from literature
- Good performance on most equivalent programs
- Finds counterexample for non-equivalent programs as well

Conclusion

Regression Verification

- Initial approach limited to strongly coupled recursions or user feedback
- Automatic Invariant Inference: More powerful, using recent techniques in SMT solvers like Eldarica and Z3

Future Work

- More examples (larger)
- Support arrays, heaps, objects